

## 2.5.D4 - LINEAR PROGRAMMING

ALL GRAPHING FOR LINEAR PROGRAMMING PROBLEMS SHOULD BE DONE ON [WWW.DESMOS.COM](http://WWW.DESMOS.COM)

For each of the following problems:

- Write a function to be minimized:  $f(x, y)$
- Write a system of inequalities:  $x \geq 0, y \geq 0$
- Graph on Desmos and then find the coordinates of the vertices of the feasible region and substitute them into the function from part a.
- Answer the problem.

- The student activities department of a community college plans to rent buses and vans for a spring break trip. Each bus has 40 regular seats and 1 handicapped seat; each van has 8 regular seats and 3 handicapped seats. A total of 320 regular and 36 handicapped seats are required for the trip.

The activities department wishes to keep costs low. The rental cost is \$350 for each van and \$975 for each bus. How many vehicles of each type should be rented to minimize cost? What is the minimum cost?

**Let  $x$  = the number of buses; let  $y$  = the number of vans.**

Write a system of equations & a function to be minimized:

	$x$	$y$	Total
$f(x, y) =$			

Find the coordinates & the vertices & evaluate:

$(x, y)$	$f(x, y)$

Answer the problem:

- A large institution is preparing lunch menus containing foods A and B. The specifications for the two foods are given in the following table:

	Units of Fat/Ounce	Units of Carbs/Ounce	Units of Protein/Ounce
Food A	1	2	1
Food B	1	1	1

Each lunch must provide at least 6 units of fat per serving, at least 10 units of carbohydrates, and no more than 7 units of protein.

The institution can purchase food A for \$0.12 per ounce and food B for \$0.08 per ounce. How many ounces of each food should a serving contain to meet the dietary requirements for the least cost?

**Let  $x$  = the ounces of food A;  $y$  = ounces of food B**

Write a system of equations & a function to be minimized:

	$x$	$y$	Total
$f(x, y) =$			

Find the coordinates & the vertices & evaluate:

$(x, y)$	$f(x, y)$

Answer the problem:

3. Johnson's Produce is purchasing fertilizer with two nutrients: N (nitrogen) and P (phosphorus). They need at least 180 units of N and 90 units of P. Their suppliers has two brands of fertilizer for them to buy. Brand A has 4 units of N and 1 unit of P. Brand B has 1 unit of each nutrient.

Brand A costs \$10 a bag while Brand B costs \$5 a bag. If Johnson's Produces wishes to minimize costs, how many bags of each brand should be purchased? How much will it cost?

**Let  $x$  = number of bags of Brand A;  $y$  = number of bags of Brand B**

Write a system of equations & a function to be minimized:

	$x$	$y$	Total
$f(x, y) =$			

Find the coordinates & the vertices & evaluate:

$(x, y)$	$f(x, y)$

Answer the problem:

4. A banquet hall offers two types of tables for rent: rectangular tables and round tables. The rectangular tables sit 6 people; the round tables provide seating for 10 people. Kathleen would like to rent the hall for a wedding banquet and needs tables for 250 people. The room can have a maximum of 35 tables and the hall only has 15 rectangular tables available.

Kathleen would like to keep her costs as low as possible. A rectangular table costs \$28 each and the round tables cost \$52 each. How many of each type of table should be rented to minimize cost and what is the minimum cost?

**Let  $x$  = the number of 6-person/rectangular tables;  $y$  = the number of 10-person/round tables**

Write a system of equations & a function to be minimized:

	$x$	$y$	Total
$f(x, y) =$			

Find the coordinates & the vertices & evaluate:

$(x, y)$	$f(x, y)$

Answer the problem: