Chapter 4: Exponential Functions

4REV.1~Lessons 4.1 & 4.2

Find the growth *factor* or decay *factor*.

- 1. A city's population increases by 17% each year.
- 2. A rain forest shrinks in size by 8.5% each year.
- 3. Water usage is lowered by 0.7% daily.
- 4. The polar ice caps melt by approximately 4% each decade.
- 5. Radioactive material is increasing by 0.62% per month.

Problems 6 – 12: Use the following functions.

$G(t) = 1500(0.98)^t$	$P(x) = 17(1.143)^x$	$T(x) = 320(1.025)^x$
$A(n) = 19.75(0.86)^n$	$C(x) = 490(0.975)^x$	$W(t) = 1.025(2.30)^t$

- 6. What is the initial value of C(x)? 7. What is the decay <u>rate</u> of A(n)?
- 8. What is the growth <u>rate</u> of T(x)? 9. Which functions are decreasing?
- 10. Which function is decaying fastest? 11. Which function has the greatest initial value?
- 12. Which function increases at the greatest rate of growth?

Identify the function as linear or exponential. Write a function equation of the form y = mx + b if linear and $y = a(b)^x$ if exponential.

14.

13.	x	y
	1	18
	2	12.8
	3	7.6
	4	2.4

x	y
1	14
2	19.6
3	27.44
4	38.416

Problems 15 & 16: Write a linear function of the form y = mx + b AND write an exponential function of the form $y = a(b)^x$. If necessary, round *m*, *b* & *a* to 2 decimal places; round *b* to 3 decimal places.

Name: _

Past due on: Period:

- 17. Halloween Town currently has 600 residents at t = 0, with t in years.
 - a. If the population grows by 80 creatures each year, find the appropriate function formula for the population, *P*, at time *t*.
 - b. If the population grows by 8% each year, find the appropriate function formula for the population, *P*, at time *t*.

Problems 18 – 22: Model the data with an <u>exponential</u> function and answer the given questions. *Round values of a to 1 decimal place and change factors, b, to 3 decimal places.*

- 18. According to the World Health organization, the population of the United States was 298.2 million in 2005. Between 1994 and 2004, the population grew at an average rate of 0.9% annually.
 - a. Model the U.S. population, P(t), as a function of the <u>years since 2005</u>, *t*.
 - b. Assuming the percentage growth rate remains the same, what is the population today?
- 19. Between 1960 and 2004, the total national expenditure on health costs increased by roughly 10.1% annually. In 1960, national health expenditures were \$28 billion.
 - a. Model the national health expenditures, E(t), as a function of the <u>years since 1960</u>, *t*.
 - b. Assuming the percentage growth rate remains the same, what was the national health expenditure in 2004?
- 20. A typical can of Mountain Dew contains 170 milligrams of caffeine. Each hour 14.5% of the amount of caffeine in the body is metabolized and eliminated.
 - a. Model the amount of caffeine in the body, C(t), as a function of the time, t.
 - b. How much caffeine remains in the body after 3 hours?
- 21. In 1985, the average NBA salary was \$325 thousand and in 1998 it was \$2600 thousand.
 - a. Model the average NBA salary, S(t), as a function of the <u>years since 1980</u>, *t*.
 - b. What is the growth <u>rate</u>?
- 22. In 1982 there were 986.8 million acres of farmland in the United States. By 1997, it had decreased to 931.8 million acres.
 - a. Model the amount of farmland, A(t), as a function of the <u>years since 1980</u>, *t*.
 - b. What is the decay <u>rate</u>?