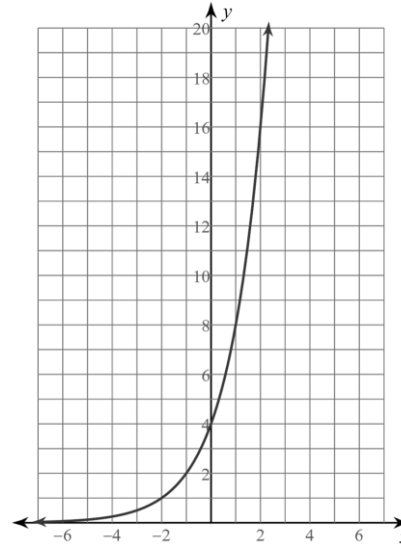
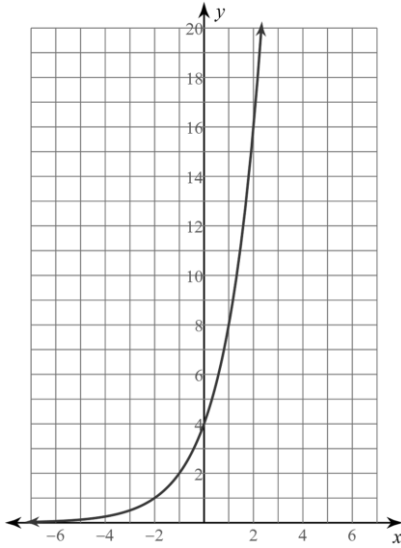


# 5.4.D2 - REFLECTIONS OF EXPONENTIAL FUNCTIONS

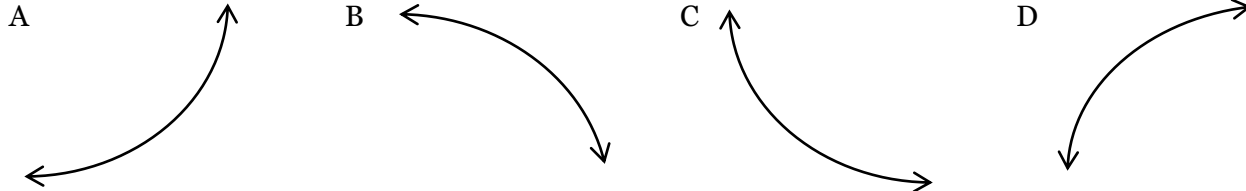
The graph of the function  $f(x) = 4(2)^x$  is given. Describe the transformations of  $g(x)$  and then sketch its graph. Refer to the 5.3 examples "Translating Exponential Functions Vertically & Horizontally" and the 5.4 example "Reflecting Exponential Functions" in the Chapter 5 Summary.

1.  $g(x) = f(-x)$

2.  $g(x) = f(x - 2) + 3$



The diagram below shows general shapes of exponential graphs.



3. Think about the shape of the graph of an exponential function of the form  $y = a(b)^x$  and the values of  $a$  and  $b$ : Is  $a$  positive or negative? Is  $b > 1$  or  $0 < b < 1$ ? Describe the values of  $a$  and  $b$  for each graph shape given.

	GRAPH A	GRAPH B	GRAPH C	GRAPH D
$a$				
$b$				

Identify, by letter, the shape of the graph for each function.

4.  $f(x) = -4^x$

5.  $g(x) = 5^x$

6.  $h(x) = 0.3^x$

7.  $p(x) = -\left(\frac{1}{2}\right)^x$

8.  $q(x) = 3\left(\frac{1}{10}\right)^x$

9.  $r(x) = -\frac{1}{5}(3)^x$

10. A function has the following points:  $G(1, -5)$ ,  $H(3, -3)$ , &  $I(5, -3)$  and has been translated 6 units left and 1 unit up. What are the coordinates of the new points?

11. A function has the following points  $K(-5, -5)$ ,  $L(5, -4)$ , &  $I(-2, -4)$  and has been reflected over the  $y$ -axis. What are the coordinates of the new points?
12. A function has the following points  $R(-5, 0)$ ,  $S(-3, 1)$ , &  $T(-4, -4)$  and has been reflected over the  $x$ -axis and shifted left 2 units. What are the coordinates of the new points?

**Problems 13 – 20: Linear or Exponential? For the linear set, write a linear function of the form  $y = mx + b$ ; for the exponential set, write an exponential equation of the form  $y = a(b)^x$ .**

13. A population has size 5000 at time  $t = 0$ , with  $t$  in years.
- If the population decreases by 100 people per year, find a function formula for the population,  $P$ , at time  $t$ .
  - If the population decreases by 8% per year, find a function formula for the population,  $P$ , at time  $t$ .
14. Write a linear or exponential function formula for the price  $p$  of a gallon of gas in  $t$  days if the price is \$2.50 on day  $t = 0$  and the price is...
- Increasing by \$0.03 per day.
  - Decreasing by \$0.07 per day.
  - Increasing by 2% per day.
  - Decreasing by 4% per day.

Examine the output pattern to determine which of the following data sets are linear and which are exponential. For the linear set, write a linear function of the form  $y = mx + b$ ; for the exponential set, write an exponential equation of the form  $y = a(b)^x$ .

15.

$x$	-2	-1	0	1	2	3	4
$y$	$\frac{1}{9}$	$\frac{1}{3}$	1	3	9	27	81

16.

$x$	-2	-1	0	1	2	3	4
$y$	2	2.5	3	3.5	4	4.5	5

17.

$x$	-2	-1	0	1	2	3	4
$y$	0.75	1.5	3	6	12	24	48

18.

$x$	-2	-1	0	1	2	3	4
$y$	0.50	2	8	32	128	512	2048

19.

$x$	-2	-1	0	1	2	3	4
$y$	6.25	2.5	1	0.4	0.16	0.064	0.0256

20.

$x$	-2	-1	0	1	2	3	4
$y$	2.5	3.75	4	5.25	6.50	7.75	8