Chapter 5: Triangles & Congruence

Name:

## 5.8 ~ Isosceles Triangles in Proofs

1. If  $\triangle HJK$  is equilateral, what are the values of *x* and *y*?



3. Given: isosceles  $\triangle ABC$  with base  $\overline{BC}$ ,  $m \angle 1 = 5x, m \angle 3 = 2x + 12$ Find:  $m \angle 2$ 



5. Given: AB = x + 3, AC = 3x + 2, BC = 2x + 3; the perimeter of  $\triangle ABC = 20$ Find the value of *x* and show that  $\triangle ABC$  is scalene.





4. Given: RS = x + 7, RT = 3x + 5, ST = 9 - xIf  $\triangle RST$  is isosceles, is it also equilateral? Explain your reasoning.



- 6. Given:  $\overline{AC} \perp \overline{BC}$ ,  $\angle C = 3x$ , BC = x + 20, & AC = 2x - 20
  - a. Find the value of *x*.
  - b. Is  $\triangle ABC$  isosceles? Explain your reasoning.



- 7. An isosceles triangle has base angles that measure  $7x^2 \& 3 20x$ .
  - a. Set up and solve a quadratic equation to find the value of *x* that makes sense.
  - b. What are the measures of all three angles?

С

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Given:  $\odot 0$ 8. D Explain why is  $\triangle COD$  is isosceles.  $\cap$ Find the indicated angle measures. 9. С kb <u>68</u>° d а т Given: D 10.  $\overline{AD} \& \overline{CD}$  are legs of isosceles  $\triangle ACD$  $\overline{DB}$  is a median  $\triangle ADB \cong \triangle CDB$ Prove:

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11. Given:  $\overline{JF} \cong \overline{JG}$   $F \text{ and } G \text{ trisect } \overline{EH}$   $\angle EFJ \cong \angle HGJ$ Prove:  $\triangle EHJ \text{ is isosceles}$ 





12. Given:  $\overline{KR} \cong \overline{PR}$  $\angle KRM \cong \angle PRO$ Prove:  $\overline{RM} \cong \overline{RO}$ 



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