Algebra 2 – Things to Remember!						
Exponents:	Complex Numbers:	Logarithms Properties of Logs.				
$r^{0} = 1$ $r^{-m} = \frac{1}{1}$	$\sqrt{-1} = i \qquad \sqrt{-a} = i\sqrt{a}; a \ge 0$	$y = \log_b x \Leftrightarrow x = b^y \qquad \qquad \log_b b = 1 \qquad \log_b 1 = 0$				
$x^{m} \bullet x^{n} = x^{m+n} \qquad \qquad x^{m} = x^{m}$ $x^{m} \bullet x^{n} = x^{m+n} \qquad \qquad (x^{n})^{m} = x^{n \bullet m}$ $\frac{x^{m}}{x^{n}} = x^{m-n} \qquad \qquad \left(\frac{x}{y}\right)^{n} = \frac{x^{n}}{y^{n}}$ $(xy)^{n} = x^{n} \bullet y^{n}$	$i^{2} = -1$ $i^{14} = i^{2} = -1$ divide exponenting by 4, use remainder, solve (a + bi) conjugate (a - bi) (a + bi)(a - bi) = a^{2} + b^{2} $ a + bi = \sqrt{a^{2} + b^{2}}$ absolute value=magning	$\ln x = \log_e x \text{ natural log} \qquad \log_b (m \cdot n) = \log_b m + \log_b n$ $e = 2.71828$ $\log x = \log_{10} x \text{ common log} \qquad \log_b \left(\frac{m}{n}\right) = \log_b m - \log_b n$ Change of base formula: $\log_b a = \frac{\log a}{\log b} \qquad \log_b (m^r) = r \log_b m$ Domain: $\log_b x \text{ is } x > 0$				
Factoring:	Exponentials $e^x = \exp(x)$	Quadratic Equations: $ax^2 + bx + c = 0$ (Set = 0.)				
Look to see if there is a GCF (greatest	$b^x = b^y \rightarrow x = y \ (b > 0 \text{ and } b \neq 1)$	Solve by factoring, completing the square, quadratic formula.				
common factor) IIISL $ab + ac = a(b + c)$	If the bases are the same, set the	$b^2 - 4ac > 0$ two real unequal roots				
$x^2 - a^2 = (x - a)(x + a)$	exponents equal and solve.	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2}$ $b^2 - 4ac = 0$ repeated real roots				
$(x+a)^2 = x^2 + 2ax + a^2$	Solving our operation equations	$b^2 - 4ac < 0$ two complex roots				
$(x-a)^2 = x^2 - 2ax + a^2$	1 Isolate exponential expression	Square root property: If $x^2 = m$ then $x = \pm \sqrt{m}$				
Factor by Grouping:	2. Take <i>log</i> or <i>ln</i> of both sides.	Completing the square: $x^2 - 2x - 5 = 0$ 1. If other than one, divide by coefficient of x^2				
144144	3. Solve for the variable.					
$x^3 + 2x^2 - 3x - 6$		2. Move constant term to other side $x^2 - 2x = 5$				
$(r^{3}+2r^{2})-(3r+6)$ group	$\ln(x)$ and e^x are inverse functions	3. Take half of coefficient of x, square it, add to both sides $\frac{2}{3} = 2 + \frac{1}{3} = 5 + \frac{1}{3}$				
(x + 2x) ($(x + 0)$ group	$\ln e^x = x \qquad e^{\ln x} = x$	$x^{-} - 2x + [\mathbf{I}] = 5 + [\mathbf{I}]$				
x(x+2) = 5(x+2) factor each	$\ln e = 1 \qquad e^{\ln 4} = 4$	4. Factor perfect square on left side. $(x-1) = 6$ 5. Use square root property to solve and get two answers. $x = 1 \pm \sqrt{6}$				
$(x^{2}-3)(x+2)$ factor	$e^{2\ln 3} = e^{\ln 3^2} = 9$					
Variation: always involves the constant of proportionality, <i>k</i> . Find <i>k</i> , and then proceed.	Absolute Value: $ a > 0$	Sum of roots : $r_1 + r_2 = -\frac{b}{a}$ Product of roots : $r_1 \cdot r_2 = \frac{b}{a}$				
Direct variation: $y = kx$	$ a = \begin{cases} a; & a \ge 0 \end{cases}$	Inequalities: $x^2 + x - 12 \le 0$ Change to =, factor, locate				
Inverse variation: $y = k$	$\left -a; a < 0 \right $	critical points on number line, check each section.				
$\begin{bmatrix} 111 \\ x \end{bmatrix}$	$ m = b \implies m = -b \text{ or } m = b$	(x+4)(x-3) = 0				
Varies jointly: $y = kxj$	$ m < b \implies -b < m < b$	x = -4; x = 5				
Combo: Sales vary directly $v = \frac{ka}{k}$	$ m > h \rightarrow m > h \text{ or } m < -h$	false true false				
with advertising and inversely <i>c c</i>		ANSWER: $-4 \leq x \leq 3$ or $[-4, 3]$ (in interval notation)				

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Radicals: Remember to use fractional exponents.	Working with Rationals (Fractions):		Solving Rational Equations:
$a \int \frac{1}{a} \frac{m}{m} n \int \frac{m}{m} (n \int)^m$	Simplify:		Get rid of the denominators by mult. all terms by
$\sqrt[n]{x} = x^{a} \qquad \qquad x^{n} = \sqrt[n]{x^{m}} = \left(\sqrt[n]{x}\right)$	remember to look for a factoring	g of -1:	common denominator.
	3x-1 - 1(-3x+1) - 1		$\frac{22}{-3} = \frac{2}{-3}$
$\sqrt[n]{a^n} = a$ $\sqrt[n]{ab} = \sqrt[n]{a} \cdot \sqrt[n]{b}$ $\sqrt[n]{\frac{1}{b}} = \frac{1}{\sqrt[n]{b}}$	$\frac{1-3x}{1-3x} = \frac{1-3x}{1-3x}$		$2x^2 - 9x - 5$ $2x + 1$ $x - 5$
Simplify : look for perfect powers.	Add: Get the common denomin	ator.	multiply all by $2x^2 - 9x - 5$ and get
$\int \frac{1}{\sqrt{r^{12} r^{17}}} = \int \frac{r^{12} r^{16} r^{1$	Factor first if possible:		22-3(x-5) = 2(2x+1)
$\sqrt{x} y = \sqrt{x} y y = x y \sqrt{y}$	Multiply and Divide: Factor Fi	rst	22 - 3x + 15 = 4x + 2
$\sqrt[3]{72x^9y^8z^3} = \sqrt[3]{8 \cdot 9x^8xy^8z^3} = 2x^2y^2z\sqrt[3]{9x}$	Rational Inequalities		37 - 3r = 4r + 2
Use conjugates to rationalize denominators:	$x^2 - 3x - 15$		37 - 3x = 1x + 2 35 - 7x
$5 2-\sqrt{3} - 10-5\sqrt{3} - 10-5\sqrt{3}$	$\frac{x-2}{x-2} \ge 0$ The critical value	ues	55 = 7x
$\frac{1}{2+\sqrt{3}} \cdot \frac{1}{2-\sqrt{3}} = \frac{1}{4-2\sqrt{3}+2\sqrt{3}-\sqrt{9}} = 10-3\sqrt{3}$	from factoring the numerator are	e -3, 5.	5 = x
Equations: isolate the radical; square both sides	The denominator is zero at $x = 2$.		Great! But the only problem is that $y = 5$ does not CHECKIIII. There is no solution
to eliminate radical; combine; solve.	Place on number line, and test s	ections.	x = 5 does not CHECK!!!! There is no solution.
$2x - 5\sqrt{x} - 3 = 0 \rightarrow (2x - 3)^2 = (5\sqrt{x})^2$	• • • • • • • • • • • • • • • • • • •	→ →	Motto: Always CHECK ANSWERS.
$4r^2 - 12r + 9 - 25r \rightarrow solve \cdot r - 9 \cdot r - 1/4$	-3 0 2 5	1	
$\frac{1}{2}x + y = 25x + y = 50000 + x = 9, x = 17 + 100000 + 100000 + 100000 + 100000 + 100000 + 100000 + 10000 + 10000 + 100000 + 100000 + 100000 + 100000 + 100000 + 100000 + 100000 + 100000 + 100000 + 1000000 + 1000000 + 1000000 + 100000000$	Sequences	Equations of Circles: $x^2 + y^2 = r^2$ center origin	
$\int dx $	Arithmetic: $a_n = a_1 + (n-1)d$	$(x-h)^2$	$(2^{2} + (y-k)^{2} = r^{2}$ center at (h,k)
Functions: A function is a set of ordered pairs in which	$S = \frac{n(a_1 + a_n)}{n(a_1 + a_n)}$	$x^2 + y^2$	+Cx + Dy + E = 0 standard form
each <i>x</i> -element has only ONE <i>y</i> -element associated with it.	\sum_{n} 2	Compl	ex Fractions:
Vertical Line Test is this graph a function?	Geometric: $a_n = a_1 \cdot r^{n-1}$	Remen	ber that the fraction bar means divide:
Domain: x-values used: Range: y-values used	$a_1(1-r^n)$	Method	11: Get common denominator top and bottom
Onto: all elements in B used.	$S_n = \frac{1}{1-r}$	2 4	2-4x
1-to-1: no element in B used more than once.	Recursive: Example:	$\frac{1}{x^2}$	$x = \frac{x^2}{x^2} = \frac{2-4x}{x^2} + \frac{4x-2}{x^2} = \frac{2-4x}{x^2} + \frac{x^2}{x^2} = -1$
Composition: $(f \circ g)(x) = f(g(x))$	$a_1 = 4; a_n = 2a_{n-1}$	4 2	$-\frac{4x-2}{x^2}$ x^2 x^2 x^2 x^2 $4x-2$
Inverse functions $f \& g: f(g(x)) = g(f(x)) = x$			· ·
		$\frac{1}{x} - \frac{1}{x^2}$	x^2
Horizontal line test: will inverse be a function?		$\frac{-}{x} \frac{-}{x^2}$ Method	x^2 1 2: Mult. all terms by common denominator for
Horizontal line test: will inverse be a function?		$\begin{bmatrix} -x & -x^2 \\ x & x^2 \end{bmatrix}$ Method all.	x^2 d 2: Mult. all terms by common denominator for
Horizontal line test: will inverse be a function? Transformations:	Binomial Theorem:	$\begin{bmatrix} -\frac{1}{x} & -\frac{1}{x^2} \\ \text{Method} \\ \text{all.} \\ \frac{2}{x^2} & -\frac{4}{x^2} \end{bmatrix}$	12: Mult. all terms by common denominator for $x^{2} \cdot \frac{2}{x^{2}} - x^{2} \cdot \frac{4}{x^{2}} = 2 - 4x$
Horizontal line test: will inverse be a function? Transformations: -f(x) over x-axis; $f(-x)$ over y-axis	Binomial Theorem: $(a+b)^{n} = \sum_{k=1}^{n} \binom{n}{2} a^{n-k} b^{k}$	$\begin{bmatrix} -\frac{1}{x} & -\frac{1}{x^2} \\ \text{Method} \\ \text{all.} \\ \frac{2}{x^2} - \frac{4}{x} \\ \frac{4}{x^2} & -\frac{4}{x^2} \end{bmatrix}$	12: Mult. all terms by common denominator for $= \frac{x^2 \cdot \frac{2}{x^2} - x^2 \cdot \frac{4}{x}}{\frac{4}{x^2} - \frac{2}{x^2}} = \frac{2 - 4x}{4 - 2} = -1$
Horizontal line test: will inverse be a function? Transformations: -f(x) over x-axis; $f(-x)$ over y-axis f(x+a) horizontal shift; $f(x)+a$ vertical shift	Binomial Theorem: $(a+b)^{n} = \sum_{k=0}^{n} {n \choose k} a^{n-k} b^{k}$	$\frac{\overline{x}}{x} \frac{\overline{x}^{2}}{x^{2}}$ Method all. $\frac{2}{\frac{x^{2}}{x}} - \frac{4}{\frac{x}{x}}$ $\frac{4}{\frac{2}{x}} - \frac{2}{\frac{2}{x}}$	12: Mult. all terms by common denominator for $= \frac{x^2 \cdot \frac{2}{x^2} - x^2 \cdot \frac{4}{x}}{x^2 \cdot \frac{4}{x^2} - x^2 \cdot \frac{2}{x^2}} = \frac{2 - 4x}{4x - 2} = -1$



Statistics and Probability -Things to Remember! Statistics: $mean = \overline{x} = \frac{x_1 + x_2 + \dots + x_n}{n} = \frac{1}{n} \sum_{i=1}^{n} x_i$ *median* = middle number in ordered data *mode* = value occurring most often *range* = difference between largest and smallest mean absolute deviation (MAD): population MAD = $\frac{1}{n} \sum_{i=1}^{n} |x_i - \overline{x}|$ variance: population variance = $(\sigma x)^2 = \frac{1}{n} \sum_{i=1}^{n} (x_i - \overline{x})^2$ standard deviation: *population* standard deviation =

 $\sigma x = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_i - \overline{x})^2}$

Sx = sample standard deviation σ_x = population standard deviation



Binomial Probability ${}_{n}C_{r} \bullet p^{r} \bullet q^{n-r}$ "**exactly**" *r* times or $\binom{n}{r} \bullet p^{r} \bullet (1-p)^{n-r}$ [TI Calculator: binompdf(*n*, *p*, *r*)]

When computing "**at least**" and "**at most**" probabilities, it is necessary to consider, in addition to the given probability,

• all probabilities larger than the given probability (**"at least**") [TI Calculator: 1 – binomcdf(*n*, *p*, *r*-1)]

• all probabilities smaller than the given probability ("**at most**") [TI Calculator: binomcdf(*n*, *p*, *r*)]

Probability Permutation: without replacement and order matters

$$_{n}P_{r}=\frac{n!}{(n-r)!}$$

Combination: without replacement and order does not matter

$$_{n}C_{r} = \binom{n}{r} = \frac{nP_{r}}{r!} = \frac{n!}{r!(n-r)!}$$

Empirical Probability $P(E) = \frac{\text{\# of times event } E \text{ occurs}}{\text{total \# of observed occurrences}}$

Theoretical Probability $P(E) = \frac{n(E)}{n(S)} = \frac{\text{\# of outcomes in } E}{\text{total \# of outcomes in } S}$

$$P(A \text{ and } B) = P(A) \bullet P(B)$$

for independent events
$$P(A \text{ and } B) = P(A) \bullet P(B|A)$$

for dependent events

$$P(A') = 1 - P(A)$$

P(A or B) = P(A) + P(B) - P(A and B)for not mutually exclusive

$$P(A \text{ or } B) = P(A) + P(B)$$

for mutually exclusive

 $P(B | A) = \frac{P(A \text{ and } B)}{P(A)}$ (conditional)