

Show that $\cos^3 x \sin^4 x$ may be converted to the expression $(1 - \sin^2 x) \sin^4 x \cos x$

$$\cos^3 x \sin^4 x = \cos x \cos^2 x \sin^4 x$$

$$\cos x (1 - \sin^2 x) \sin^4 x$$

Show that the first expression is equivalent to the second:

$$\frac{\cot^2 \beta + \sec^2 \beta + 1}{\cot^2 \beta} = \sec^4 \beta$$

$$\frac{\cot^2 \beta + \tan^2 \beta + 1 + 1}{\cot^2 \beta}$$

Apply the Pythagorean Identity:
 $\tan^2 \theta + 1 = \sec^2 \theta$

$$\frac{\cot^2 \beta + \tan^2 \beta + 2}{\cot^2 \beta}$$

Rewrite everything in terms of tangent.

$$\frac{\frac{1}{\tan^2 \beta} + \tan^2 \beta + 2}{\frac{1}{\tan^2 \beta}}$$

When confronted w/a complex fraction, multiply all terms by the common denominator of the "mini fractions."

$$\left(\frac{\frac{1}{\tan^2 \beta} + \tan^2 \beta + 2}{\frac{1}{\tan^2 \beta}} \right) \times \tan^2 \beta$$

$$\frac{1 + \tan^4 \beta + 2 \tan^2 \beta}{1}$$

Factor the numerator. Pretend it's:
 $x^4 + 2x^2 + 1 = (x^2 + 1)(x^2 + 1)$

$$(\tan^2 \beta + 1)(\tan^2 \beta + 1)$$

Apply the Pythagorean Identity:
 $\tan^2 \theta + 1 = \sec^2 \theta$

$$(\sec^2 \beta)(\sec^2 \beta)$$

$$\sec^4 \beta$$